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Neutral magnesium as a probe of high column density QSO absorbers.

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NEUTRAL MAGNESIUM AS A PROBE OF
HIGH COLUMN DENSITY QSO ABSORBERS

By

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A Thesis
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For the Degree of

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University of Louisville
Louisville, Kentucky

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further. Lastly, I’m eternally indebted to Amanda Houpt for her love, understanding, and partnership.
ABSTRACT

NEUTRAL MAGNESIUM AS A PROBE OF

HIGH COLUMN DENSITY QSO ABSORBERS

Joseph N. Burchett

April 14, 2011

QSOs, providing distant, luminous sources of radiation, provide a means to detect gas by absorption in the interstellar and intergalactic medium. Of particular interest to astronomers studying metal line systems in lines of sight to QSOs are the classes characterized by their neutral hydrogen column density known as Damped Lyman-α systems (DLAs) and Sub-damped Lyman-α systems (Sub-DLAs). DLAs and Sub-DLAs provide a means to probe the detailed abundance and dust content of the Universe at high redshift, revealing the evolving presence of elements heavier than hydrogen and helium. Here, we present a correlation between ionization and metallicity as indicated by the abundance ratios [Si II / Mg I] and [Zn II / HI], respectively, in such systems at redshift $z\sim0.5-2.7$. The abundances used were drawn from the literature where reported. However, where elemental abundances were omitted in the literature, we profile fit those spectra to obtain them. We believe that this correlation, if proven valid, could provide another tracer of evolution of elements throughout the history of the Universe.
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SECTION I

INTRODUCTION AND BACKGROUND

It is well known that the volume between stars and even between galaxies is far from empty; the interstellar medium (ISM) and intergalactic medium (IGM) are key areas of focus for astronomers studying star formation, the formation and evolution of galaxies, and cosmology. However, these regions contain gas and dust representing a diversity of composition, temperature, and bulk kinetic properties. Various techniques are employed to study the ISM/IGM, largely dependent on the phase and/or dynamics of the system under scrutiny.

For instance, radio telescopes may be used to observe interstellar carbon monoxide (CO) and other molecules which produce emission in dense regions at long wavelengths. Also, neutral hydrogen (HI) is observed at the 21cm wavelength in emission when found in warm gas regions and in absorption when in cold gas. Cold, dusty regions are best observed in the far-infrared regime where wavelengths exceed the sizes of dust grains which lead to the obscuration of “bluer”, smaller wavelength photons. In the optical and UV regimes, another technique is to derive the chemical and physical conditions (elemental abundances, density, ionization state, etc.) in individual components for gas clouds when they happen to lie in the line of sight to a more distant star or luminous object as is illustrated in Figure 1. The data presented in this study were obtained in this manner.
Photons emitted from the background radiation source are absorbed by atoms, molecules, and ions in the intervening gas, resulting in a spectrum that shows the "fingerprint" of the chemical composition of the gas. This results from photoexcitation from one quantum mechanical state to another or from photoionization where electrons in bound states are supplied with enough energy to be freed. The energy required for these transitions correspond to specific wavelengths of light by the familiar relation:

\[ E = \frac{hc}{\lambda} \]
Interpretation of spectra lies at the heart of observational astronomy and the remainder of the first part of this thesis serves as an overview in relevant context and the mathematical underpinning.

**QSO Spectral Features**

All of the sight lines for these data contain gas clouds that are seen against quasi-stellar objects (QSOs) in the background. QSOs are luminous, distant objects that emit radiation due to supermassive black holes in host *active galactic nuclei* (AGN) which constantly accrete material while also expelling material in powerful jets. The designation ‘QSO’ is used here but the term ‘quasar’ may also be encountered in similar context although a quasar is defined as being a quasi-stellar radio source (Carroll & Ostlie 2007). This ambiguity is of little consequence in this paper and is only mentioned for semantic reasons as the radio region of the electromagnetic spectrum is not used here.

Absorption lines in the continuum radiation emitted by the QSO reveal a wealth of information about the gas clouds that lie between Earth and the QSO. Figure 2 shows an example QSO spectrum which displays several characteristic properties.
Notice the particularly strong peak at 2850 angstroms. This peak corresponds to the Lyman-α (n=2 to n=1) energy transition of the hydrogen atom which has magnitude $\Delta E = 10.2$ eV. While this transition corresponds to a wavelength of 1215.6 Å in the lab frame, the line has been *cosmologically redshifted* due to the expansion of the Universe. The relation between the transition wavelength in the lab frame to the observed (redshifted) wavelength is:

$$\lambda_{\text{obs}} = (1+z) \lambda_{\text{lab}}$$

where $z$ is the redshift of the emitting or absorbing material. Therefore, this QSO located at a redshift of 1.34 shows the Lyman-α transition centered at a wavelength of 2850 Å.

The next most profound feature of this spectrum is the dense concentration of narrow absorption lines blueward of the Lyman-α emission peak. Known as the *Lyman-α*
forest, these lines correspond to Lyman-α photoexcitation undergone by intervening, ionized gas clouds that exist at various redshifts between Earth and the QSO. Thus the Lyman-α line for each cloud is observed at a wavelength found according to $\lambda = \frac{hc}{E}$ and the equivalent width of that line indicates the amount of neutral hydrogen gas contained within the cloud and its turbulent and thermal broadening, which we will explore further when we discuss measurement of absorption lines.

Abundances of interstellar and intergalactic gas are usually expressed as column densities in units of cm$^{-2}$. This is best visualized as a mere count of the number of atoms or molecules present in a tube with cross-sectional area 1 cm x 1 cm extending from the radiation source (star, quasar, etc.) to the observer. Generally the column density is denoted by $N(X)$ where $X$ specifies the atom, molecule, or ion being measured and uses spectroscopic notation to represent ionization state such as HI (neutral hydrogen), CIV (triply-ionized carbon), etc. Certain values of column density reflect unique spectral features or serve as defining criteria of intervening clouds.

One such spectral feature, the Lyman limit (also called the Lyman break), refers to the nearly complete absorption of incident radiation at wavelengths less than 912 Å in the rest frame. This wavelength corresponds to the ionization energy ($\sim$13.6 eV) of the hydrogen atom indicating that incident photons supply enough energy to free electrons from their bound states with host nuclei. When the column density of neutral hydrogen exceeds $2 \times 10^{17}$ cm$^{-2}$, enough atoms are present to absorb (and be ionized by) photons exceeding this energy. While the rest frame wavelength of 912 Å exists in the extreme ultraviolet regime, with increasing redshift this Lyman limit is moved to redder (longer) wavelengths, leaving the shorter wavelengths devoid of flux in the spectrum. This
creates a distinct drop-off feature in the spectrum and astronomers exploit this distinct feature using methods beyond the scope of this thesis.

**Distant Objects as Tools to Study the Early Universe**

It was stated above that studying the intergalactic medium gives insight to the formation and evolution of galaxies and stars. Due to the finite speed of light \( c \approx 3 \times 10^8 \text{ m/s} \) and the expansion of the Universe, when we observe objects at greater and greater distances, we are peering further and further back in time. For instance, the Andromeda Galaxy (M31) is located approximately 800 kiloparsecs away (Sparke & Gallagher 2007), a distance that takes approximately 2.6 million years for light to travel. Thus, the photons that we detect today originated 2.6 million years ago. Considering that Andromeda is nearby on cosmological distance scales, objects much further away clearly provide insight into a younger Universe.

So, the redshift that causes absorption lines of certain transitions to be observed at longer wavelengths arise from the velocity at which objects are moving away from us. As Edwin Hubble was able to prove, this *recessional velocity* is directly related to the distance to these objects and the relation is known as Hubble’s Law:

\[
V_r \approx H_0 d
\]

Where \( V_r \) is the recessional velocity, \( H_0 \) is the Hubble constant, and \( d \) is the distance to the object.
Therefore, with increasing redshift we have a greater *lookback time*, or time since the observed light was emitted or absorbed. Though we omit a detailed discussion of the underlying cosmology, it is useful to have some reference for lookback times as they relate to common observable redshifts. A useful online tool for this is *Ned Wright’s Javascript Cosmology Calculator*\(^1\). Several redshift values and their corresponding lookback times from this online calculator are provided in Table 1. For all these calculations, we have assumed a flat universe, Hubble constant \(H_0 = 71\ \text{km s}^{-1}\ \text{Mpc}^{-1}\), \(\Omega_M = 0.27\), and \(\Omega_{\text{vac}} = 0.73\).

Also online, Wright has published the accompanying *Ned Wright’s Cosmology Tutorial*\(^2\) which is very useful for further explanation of basic cosmological concepts.

---


<table>
<thead>
<tr>
<th>$z$</th>
<th>Lookback Time (Gyr)</th>
<th>Age of Universe (Gyr)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.25</td>
<td>2.916</td>
<td>10.749</td>
</tr>
<tr>
<td>0.5</td>
<td>5.019</td>
<td>8.646</td>
</tr>
<tr>
<td>0.75</td>
<td>6.567</td>
<td>7.098</td>
</tr>
<tr>
<td>1</td>
<td>7.731</td>
<td>5.934</td>
</tr>
<tr>
<td>1.25</td>
<td>8.623</td>
<td>5.042</td>
</tr>
<tr>
<td>1.5</td>
<td>9.32</td>
<td>4.345</td>
</tr>
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<td>9.875</td>
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<td>2</td>
<td>10.324</td>
<td>3.341</td>
</tr>
<tr>
<td>2.25</td>
<td>10.692</td>
<td>2.973</td>
</tr>
<tr>
<td>2.5</td>
<td>10.999</td>
<td>2.666</td>
</tr>
<tr>
<td>2.75</td>
<td>11.256</td>
<td>2.409</td>
</tr>
<tr>
<td>3</td>
<td>11.476</td>
<td>2.189</td>
</tr>
<tr>
<td>4</td>
<td>12.094</td>
<td>1.571</td>
</tr>
<tr>
<td>5</td>
<td>12.469</td>
<td>1.196</td>
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<td>13.183</td>
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</tr>
<tr>
<td>100</td>
<td>13.649</td>
<td>0.016</td>
</tr>
</tbody>
</table>

Table 1: Lookback time and age of the Universe at various redshifts, assuming a flat Universe with $H_0 = 71 \text{ km s}^{-1} \text{ Mpc}^{-1}$, $\Omega_M = 0.27$, and $\Omega_{\text{tot}} = 0.73$ (Ned Wright's Javascript Cosmology Calculator)
Measurement of Absorption Lines

As stated above, absorption lines occur in a spectrum due to energy transfer from incident radiation to the absorbing material. Above, we mentioned some specific transitions associated with the hydrogen atom, but QSO absorption line spectroscopy concerns itself with any observable element. Table 2 lists several commonly seen transitions and wavelengths at which we might detect their presence by absorption.

Beyond the identity of elements present and their ionization states, we can also measure abundances of these species in absorption lines. Figure 3 shows an (highly idealized) example of an absorption line where the vertical scale is the intensity of the measured radiation and the horizontal scale, although labeled as frequency, may be interpreted as either frequency or wavelength.

![Figure 3: Evaluation of the equivalent width. The shaded rectangle is constructed to span from the continuum to the zero-flux axis such that the two shaded areas are equal. The equivalent width is defined as the width of this rectangle.](image_url)
<table>
<thead>
<tr>
<th>Element/Ion</th>
<th>( \lambda (\text{Å}) )</th>
<th>( f )</th>
</tr>
</thead>
<tbody>
<tr>
<td>H I</td>
<td>1215.6701</td>
<td>0.416400</td>
</tr>
<tr>
<td>C IV</td>
<td>1548.1950</td>
<td>0.190800</td>
</tr>
<tr>
<td></td>
<td>1550.7700</td>
<td>0.095220</td>
</tr>
<tr>
<td>Si II</td>
<td>1808.0130</td>
<td>0.002186</td>
</tr>
<tr>
<td>Zn II</td>
<td>2026.1360</td>
<td>0.489000</td>
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<tr>
<td></td>
<td>2062.6640</td>
<td>0.256000</td>
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<tr>
<td></td>
<td>2026.4768</td>
<td>0.113000</td>
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<tr>
<td>Mg I</td>
<td>2852.9642</td>
<td>1.810000</td>
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<tr>
<td>Cr II</td>
<td>2056.2539</td>
<td>0.105000</td>
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<tr>
<td></td>
<td>2062.2340</td>
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<td>0.051500</td>
</tr>
<tr>
<td></td>
<td>2249.8768</td>
<td>0.001821</td>
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<tr>
<td>Fe II</td>
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<td>0.002440</td>
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<tr>
<td></td>
<td>2344.2140</td>
<td>0.114000</td>
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<td>2374.4612</td>
<td>0.031300</td>
</tr>
<tr>
<td></td>
<td>2382.7650</td>
<td>0.320000</td>
</tr>
<tr>
<td></td>
<td>2584.6500</td>
<td>0.069100</td>
</tr>
<tr>
<td></td>
<td>2600.1729</td>
<td>0.239000</td>
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<tr>
<td></td>
<td>2576.8770</td>
<td>0.350800</td>
</tr>
<tr>
<td>Mn II</td>
<td>2594.4990</td>
<td>0.271000</td>
</tr>
<tr>
<td></td>
<td>2796.3520</td>
<td>0.612300</td>
</tr>
<tr>
<td>Mg II</td>
<td>2796.3543</td>
<td>0.615500</td>
</tr>
<tr>
<td></td>
<td>2803.5310</td>
<td>0.305400</td>
</tr>
</tbody>
</table>

Table 2: Wavelengths and oscillator strengths of atomic transitions.

The incident radiation field on the absorbing material forms a continuum, labeled \( I_0 \) on the vertical axis. In the normalization process with a real spectrum, we would fit a polynomial function to the continuum. To the right of the absorption line, we see a vertical strip constructed so that its area is equal to the shaded area of the region between the line and the continuum. Note that the height of this strip extends from the continuum to the axis of zero intensity. The strip's width is called the \textit{equivalent width} and may be expressed mathematically by:
\[ W = \int \left( 1 - \frac{I(\nu)}{I_0} \right) d\nu \]

Where \( I_0 \) is the continuum radiation intensity and \( I(\nu) \) is the intensity at a given frequency (Dyson & Williams 1997). It is then useful to introduce the optical depth \( \tau_\nu \) which relates both the continuum intensity and the measured (absorption) intensity by\(^3\):

\[ I(\nu) = I_{\nu0} e^{-\tau_\nu} \]

The equivalent width may then be rewritten in terms of the optical depth as:

\[ W = \int \left( 1 - e^{-\tau} \right) d\nu \]

As we wish to ultimately derive the column density of the absorbing material, we then express the optical depth as a product of the column density \( N \) and the cross-section \( \sigma \) of absorption or scattering of the incoming photons:

\[ \tau_\nu = N\sigma_\nu \]

The relationship between column density and equivalent width is then clearly dependent on the interaction cross-section of incident photons. A curve of growth is often used to depict this relationship such as that of Figure 4. For small \( N \), we may use a mean cross-section over \( \Delta\nu \) to make the following approximation:

\[ W = N\sigma_0\Delta\nu \]

\(^3\) The next four equations are adapted from The Physics of the Interstellar Medium by Dyson & Williams (Institute of Physics Publishing 1997).
This is known as the *linear portion* of the curve of growth. When the optical depth becomes "large", we see saturation that contains contribution from instrumental as well as kinematic effects (Welty, Hobbs, and Kulkarni 1974). Here the relationship between column density and equivalent width goes from $W \propto N$ to $W \propto (\ln N)^{1/2}$. We call this the *flat portion* of the curve of growth, where the column density and equivalent width have a much weaker dependence on one another. By further increasing the column density (and thus the optical depth), we begin to see damping wings in the absorption line and the curve of growth enters the *square root portion*, so-called because $W \propto N^{1/2}$. In this region, the uncertainty of the measured column density dramatically decreases.

![Figure 4: A sample curve of growth. With increasing column density (and therefore equivalent width), we encounter the linear portion (unsaturated spectral line), the flat portion (saturated line but not possessing damping wings), then the square root portion (the line is so saturated that damping wings form). (Carroll & Ostlie 2007)](image-url)
While the preceding discussion focused on the relationship between column density and equivalent width, we now turn to the factors influencing the absorption cross-section $\sigma_v$. Interpreting the cross-section as the likelihood of an interaction, certain transitions between quantum-mechanical states are more likely than others. We quantify this likelihood by the oscillator strength $f$. For instance, the Lyman-$\alpha$ transition of the neutral hydrogen atom has an $f$-value of 0.4164 whereas the Lyman-$\beta$ has $f = 0.07914$ [Morton 2004]. Therefore, the Lyman-$\alpha$ absorption is about 5.26 times more likely to occur. For a given column density of HI, the equivalent width of the Lyman-$\alpha$ line will then be correspondingly greater. Several transitions, wavelengths, and oscillator strengths are given in Table 2.

Also contributing to the shape and size of the absorption line are physical processes that have a broadening effect\(^4\). The first contribution is from natural broadening, resulting from the Heisenberg uncertainty principle. An infinitely sharp line would imply a zero uncertainty of the wavelength (and thus energy) measurement due to a state transition, however the brief time that an electron occupies the excited state places a nonzero lower bound on the uncertainty. A second contribution comes from the interactions that the constituent particles of the gas undergo with one another, called pressure broadening. Together with natural broadening, this generates a Lorentz profile, which mathematically takes the form:

\[^4\text{This section is paraphrased from section 9.5 of An Introduction to Modern Astrophysics by Bradley W. Carroll and Dale Ostlie which in itself is marginally more mathematically rigorous. For a more complete discussion of line profiles, the reader is referred to (Spitzer 1978)}\]
\[ \Delta \lambda \approx \frac{\lambda^2}{c} \frac{n \sigma}{\pi} \sqrt{\frac{2kT}{m}} \]

The third contribution is from *thermal broadening* where we take into effect Doppler shifts due to the random motions of individual particles. Clearly, these motions are due to the thermal kinetic energy possessed by the gas and are heavily dependent on its temperature. Assuming that the gas particles are distributed as a Maxwell-Boltzmann function, the width of the line at half its maximum depth due to thermal broadening will exhibit a Gaussian profile:

\[ (\Delta \lambda)_{\text{FWHM}} = \frac{2\lambda}{c} \sqrt{\frac{2kT}{m} + \frac{v_{\text{therm}}^2}{m}} \ln 2 \]

The combined effects of these broadening mechanisms can be modeled by a convolution of the Lorentz and Gaussian profiles, known as a Voigt profile. By fitting a Voigt profile to an absorption line, we may then extract these physical parameters which give rise to its size and shape.

**Nucleosynthesis and the Enrichment of the ISM/IGM**

While the elements hydrogen, helium, lithium, and beryllium were created in the Big Bang, all elements that are heavier (atomic number > 4) are created in the inner recesses of stars. These elements are produced by the very fusion processes that generate stars' energy. Then, depending on a star's mass (and therefore ultimate fate), various mechanisms inject the surrounding space with these metals where they are they may become part of new stars, continuing the cycle.
Elements are generally classified according to the processes by which they are created. One classification is known as the alpha-process, so-called due to their formation which involves the continual fusion of $^4_2$He nuclei (α-particles). As such, the α-elements (O, Ne, Mg, Si, S, Ar, Ca and Ti) possess nuclei with even-numbers of protons. They are expelled to the ISM during Type II supernovae.

Another class of elements, called the iron-peak nuclei are bound together relatively tightly compared to other nuclei of similar masses. The name for this classification comes from the peak that occurs in binding energy per nucleon plotted against increasing atomic mass number. The ISM is enriched by the Fe-peak elements (Zn, Cr, Mn, Fe, Co and Ni) largely via Type Ia supernovae, although there is a lesser contribution from Type II SNe.
As stated in the title, this work is concerned with high column density absorption systems. The column density in question is that of neutral hydrogen, in particular where $\log N(\text{HI}) \geq 19.0$. The highest column systems of interest are those where $\log N(\text{HI}) \geq 20.3$ and are known as Damped Lyman-$\alpha$ Systems or DLAs. As the name suggests, these systems have such a high column density as to show damping wings in the Lyman-$\alpha$ absorption line which exists in the rest frame at 1215.6 Å.

A second class of systems have lower column density: $19.0 \leq \log N(\text{HI}) \leq 20.3$ and are known as sub-Damped Lyman-$\alpha$ Systems (Sub-DLAs). Here, the difference in naming is purely historical as the damping wings which characterize the DLAs are still visible in these systems but were not able to be seen in the initial low spectral resolution surveys of QSOs. As we will see in greater detail, many of these systems appear to be metal-rich. Therefore, they provide important clues into the nucleosynthetic history of the Universe (Kulkarni, et al. 2007), i.e. how the amount of metals present in stars, galaxies, and the ISM/IGM has evolved over cosmic time.

Not only is most of the hydrogen gas in DLAs and Sub-DLAs neutral, but these systems are believed to possess most of the neutral gas in the Universe (Storrie-Lombardi & Wolfe 2000, Wolfe 1995). These neutral gas clouds are the progenitors of molecular
clouds when then give way to star formation. It can be shown that DLAs and Sub-DLAs observed at earlier epochs contain enough neutral hydrogen to form all of the stars that we see today.

**Dust Depletion**

By using the absorption line method of measuring interstellar and intergalactic abundances, we concede that the resulting column densities are only a measure of these species in the *gas-phase*. However, depending on the environment (temperature and pressure) of the gas cloud and the amount present of an element or molecule, a fair amount of material may be condensed onto dust grains. Of course, measurements of the gas-phase will underreport the total amount present if some of the species is present in the form of dust. We refer to this as *depletion*.

The tendency of some atoms and molecules to be incorporated into dust grains is greater than for others. Depletions of these so-called *refractory elements* have been studied in various environments within our Galaxy and beyond (Jenkins 2009, Savage & Sembach 1996, Cartledge et al. 2006, Welty et. al 2001) and several depletion patterns are shown in Figure 5, reproduced here from Meiring et al. (2009).

Of greatest consequence to this thesis is the considerably increased depletion of Cr and Fe relative to Zn. We discuss the specifics of these consequences later in our use of observables to trace physical conditions of absorption systems.
It should be noted that the understanding of dust content is not merely to account for inaccuracies in measured abundances; dust grains play many important roles in the ISM/IGM. In the introduction, we presented an example of observing dust-obscured environments and the fact that short wavelengths are scattered by the dust grains. This has an effect on the radiation field in a gas cloud as well since energetic UV photons may be absorbed or scattered by the grains which then reradiate at longer wavelengths. Also, dust grains happen to be the sites of molecular hydrogen formation (Hollenbach & Salpeter 1971). Stars form by the collapse of molecular clouds, therefore dust has large implications in the realm of star formation.

Figure 5: Depletion patterns for several representative sight lines. Notice the small amount of depletion of Zn compared with Fe. (Meiring et al. 2009)
**Metallicity**

DLAs and Sub-DLAs offer a unique perspective into the chemical evolution of the Universe by probing the composition of dense clouds at various epochs. Of particular interest are how elements heavier than helium, the ‘metals’, came to be formed and distribute over cosmic time. We stated above that Sub-DLAs tend to be more metal-rich than DLAs, but let us now examine in greater detail the metal content of high-column absorbers, discussing means of measurement and some key observed trends.

In referring to the metallicity of a system, we shall use the relative abundance of zinc to hydrogen, \([\text{Zn}/\text{H}]\). This may call into question why we do not use iron, chromium, or another metal. Going back to the discussion of dust, we see a clear difference of depletion in the abundances of zinc, which has little to no depletion depending on the sight line, and these other aforementioned elements. Therefore, our measurement of zinc in the gas-phase is likely to represent a much more accurate measure of the total zinc in the system than a measurement of iron to its true abundance. Furthermore, Zn belongs to a set of elements known as the *iron-peak* elements and therefore traces very well the abundances of Fe, Cr, Ni, and others (Lauroesch et al. 1996).

As a picture of the evolving metal content in DLAs and Sub-DLAs, Figure 6 shows a plot of metallicity versus redshift reproduced from Wolfe, Gawiser, and Prochaska (2005). We see a clear increase in metallicity over cosmic time which is expected due to the cumulative enrichment of heavy elements into the ISM/IGM via supernova and stellar wind activity.
Abundance Ratios

In studying the physical characteristics of DLAs and Sub-DLAs, we use a variety of abundance ratios. First, to define the nomenclature (Lauroesch et al. 1996):

\[ \frac{X}{Y} = \log N(X) - \log N(Y) - \left[ \frac{X}{Y} \right]_{\text{solar}} \]

Where \(N(X)\) and \(N(Y)\) correspond to the column density of each respective element. Essentially, we are expressing the abundance of one element relative to another with that ratio relative to the same elements’ abundance ratio in the neighborhood of the Sun. As an example, a measurement of a system with \([Zn/H] = -2\) tell us that the system has
1/100\textsuperscript{th} the amount of zinc as hydrogen when compared with the same ratio as measured near the Sun.

In general, we use abundance ratios in attempts to derive physical characteristics of distant environments. In doing so, we must take into consideration the chosen elements' nucleosynthetic origins to insure that their comparison is meaningful (Lauroesch 1996, Timmes et al. 1996). This same reasoning was used above in stating that [Zn/H] would trace intrinsic (undepleted) values of [Fe/H] as a measure of metallicity (both are Fe-peak elements). As such, [Zn/Fe] may be used as an indication of dust content due to the greater depletion of Fe than that of Zn. An interesting trend is shown in Figure 7 where we see increasing dust content when plotted against metallicity. Again, this figure was originally provided in the review by Wolfe, Gawiser, and Prochaska (2005).

Figure 7: A trend of dust relating to systems' metallicity. [Zn/Fe] serves a tracer for dust content due to the high depletion of Fe while Zn remains largely undepleted.
Also, due to the high depletion of Cr, \([\text{Cr/Zn}]\) similarly provides an indication of dust content as Cr is also an Fe-peak element. Referring back to figure 4, we see that through most of the sight lines Cr and Fe display comparable depletion.

Often times, ISM/IGM constituents exist in a predominately ionized state. Measuring the extent of this ionization reveals much about incident radiation upon the system and the recombination processes that may be taking place. We use \([\text{Si II / Mg I}]\) for this study, the relative abundance of singly ionized silicon to neutral magnesium. The choice of Si II instead of Mg II is largely due to practical concerns as the lines used to measure Mg II at wavelengths 2803 Å \((f = 0.306)\) and 2795 Å \((f = 0.616)\) are generally too saturated to obtain accurate abundance measurements. In general, the \(\lambda 1808 (f = 0.0022)\) line of Si II is unsaturated and thus far more measurable (oscillator strength values obtained from Morton 2004 and Prochaska et al. 2003). Note that Si and Mg are also both \(\alpha\)-elements thus their presence results from Type II SNe enrichment.

We now conclude this section with a brief mention of some other abundance ratios and their corresponding physical implications. The first is \([\alpha / \text{Fe}]\), which is the relative abundance of the alpha-process elements \((\text{O, Ne, Mg, Si, S, Ar, Ca, Ti})\) to iron. As described in §1.3, the ISM is enriched with the \(\alpha\)-elements via Type II supernovae. While this clearly provides insight to history of star formation and death, work has also been done to include these data as parameters in models of galaxy evolution especially in the realm of dwarf spheroidal galaxies (Tolstoy & Venn 2003, Cohen & Huang 2010, Lauroesch et al. 1996).
Another useful abundance ratio is that of $\frac{[N]}{[\alpha]}$, which has been used as a tracer of a system’s age. Timmes et al. (1997) as well as Pettini, Lipman, & Hunstead (1995) suggested the use of nitrogen abundances to study age-metallicity relationships. Large $\frac{[N]}{[\alpha]}$ have been thought to be older systems since there is a predicted lag between the enrichment of $\alpha$-elements into the ISM (Type II SNe) and the infusion of nitrogen from stars on the asymptotic giant branch. This simple model is complicated however by further work (Prochaska et al. 2002) implying that the time separation between $\alpha$-enrichment and N-enrichment may not consistently result in increasing $\frac{[N]}{[\alpha]}$ with age.
SECTION III

DATA

Here we present our data sample. The sample includes 30 systems (15 DLAs and 15 Sub-DLAs), all of which had previously published abundances for H I, Zn II, and Si II. However, six of the systems did not have published abundances for Mg I, which we obtained by profile fitting using publically available spectra. More detail on these data sources will be given below as will discussion of the profile fitting procedure. Visual comparison of the abundance ratios [Si II / Mg I] and [Zn II / H I] appeared to suggest a correlation\textsuperscript{5} which we then tested and fit using survival analysis techniques. The results of our data analysis are presented in the next section and we save the discussion of potential causes of our results for the final section of this thesis.

Sources of Data

The objects in our sample are derived from observations published in ten different sources: Lopez et al. (1999), Srianand & Petitjean (1998), Prochaska & Wolfe (1999), Khare et al. (2004), Prochaska et al. (2007), Meiring et al. (2007), Peroux et al. (2002), Meiring et al. (2009), Meiring et al. (2010), and Noterdaeme (2010). While adequate

\textsuperscript{5} See figure 8
detail is given in each of these papers about their respective observations, we summarize
the telescope and instrument used for the observations in Table 3.
Figure 8: Our data sample. If viewed in color, the red points indicate a DLA whereas the blue points represent Sub-DLAs.
<table>
<thead>
<tr>
<th>QSO</th>
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<th>Instrument</th>
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</tr>
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<td>W.M. Keck</td>
<td>HIRES</td>
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<td>W.M. Keck</td>
<td>HIRES</td>
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<td>UVES, X-shooter</td>
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</tr>
<tr>
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<td>HIRES</td>
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<tr>
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<td>W.M. Keck</td>
<td>HIRES</td>
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</tbody>
</table>

Table 3: A summary of objects used in this study, including objects for which profile fitting was performed and those found in the literature.
Historically, suspected DLAs were chosen to observe more closely with high resolution spectrographs due to profound absorption features seen in low-resolution spectra as part of larger surveys. For instance, the SDSS has surveyed 25% of the sky visible from Earth. However, the spectral resolution is far too low to detect many of the weaker metal lines that are of interest for in-depth abundance studies, the MgII doublet at \(\lambda\lambda 2795, 2803\) Å is so prominent as to indicate the presence of a high column density system (Lauroesch, private communication). The observed wavelengths of these lines indicate the redshift at which the responsible absorber might lie. As an example, this doublet observed at \(\lambda\lambda 4611, 4625\) Å would suggest the possibility of a system at \(z = 0.65\):

\[
z = \frac{4625}{2803} - 1 = 0.65
\]

It should also be noted that, at such moderate redshifts, these lines fall conveniently in the optical range of the spectrum which is observable from ground-based instruments. In the rest frame, they fall in the UV which is shielded by Earth’s atmosphere.

Of these 30 objects, 24 had previously published abundances that were necessary for this study. These are listed in Table 4.
Table 4: Column Densities obtained from the literature. Although two objects are missing Cr II abundances, those values were not used in the correlation test.
Profile Fitting of Archival Spectra

The remaining six objects did not have published Mg I column densities, therefore we measured them using profile fitting software. While the H I, Si II, and Zn II abundances for these objects were all published either in Prochaska & Wolfe (1999) or Prochaska et al. (2007), the Mg I abundance was omitted. Their group has made all of these spectra (and many more) available in an online archive\(^6\), which is where we obtained them. These six were chosen from a set of 25 spectra which upon inspection, revealed the reasons for omitting Mg I due to a break in wavelength coverage, an inadequate signal-to-noise ratio, or blending with absorption from another system that made a clear measurement indiscernible. However, for six of these objects we were able to fit and obtain an Mg I column density: FJ0812+32, PH957 (Q0100+13), Q0841+12, Q1215+33, Q1331+17, and Q2231-00.

The software we used to do profile fitting is entitled FITS6P (Welty et al. 1997), written and maintained by Dan Welty with contribution from others\(^7\). FITS6P uses an iterative, least-squares procedure to fit a Voigt profile to specified absorption lines. Once specifications of the instrument and redshift of the absorber are entered, the user supplies test values of the parameters \(N\) (column density), \(b\) (Doppler parameter), and \(v\) (velocity). These may be individually varied or fixed as the fit is performed.

In general, we used the following procedure to obtain column densities for these objects. First, we isolated the region of the spectrum that contains the (rest frame) lines

\(^6\) http://msc.caltech.edu/archives/koa
\(^7\) https://netfiles.uiuc.edu/dwelty/www/soft.html
λλλ2056.5, 2062.5, 2066.4 Cr II and λ2062.9 Zn II. These lines were then simultaneously fit to obtain $N(Cr\ II), N(Zn\ II), b,$ and $v$. Then, in a separate run, we inserted these column densities as starting values to fit the λ2026.4 Cr II, λ2026.6 Zn II, and λ2026.8 Mg I lines. This method, although seemingly repetitive, is necessary to obtain the appropriate contributions from each ion in the blended line.

Figures 9-14 show our fits of these spectra. Table 5 shows the results of these measurements along with their 1σ uncertainties also calculated by FITS6P.
Figure 9: Absorption line profile fitting for FJ0812+32. The top figure represents fitting of the Cr II 2056, Cr II 2062, Zn II 2062, and Cr II 2066 lines, velocity centered on the Cr II 2056 line, while the bottom depicts fitting of the Zn II 2026, Cr II 2026, and Mg I 2026 lines, velocity centered on the Zn II line. This system has a redshift of 2.6263.
Figure 10: Absorption line profile fitting for PH957. The top figure represents fitting of the Cr II 2056, Cr II 2062, Zn II 2062, and Cr II 2066 lines, velocity centered on the Cr II 2056 line, while the bottom depicts fitting of the Zn II 2026, Cr II 2026, and Mg I 2026 lines, velocity centered on the Zn II line. This system has a redshift of 2.3090.
Figure 11: Absorption line profile fitting for Q0841. The top figure represents fitting of the Cr II 2056, Cr II 2062, Zn II 2062, and Cr II 2066 lines, velocity centered on the Cr II 2056 line, while the bottom depicts fitting of the Zn II 2026, Cr II 2026, and Mg I 2026 lines, velocity centered on the Zn II line. This system has a redshift of 2.3750.
Figure 12: Absorption line profile fitting for Q1215. The top figure represents fitting of the Cr II 2056, Cr II 2062, Zn II 2062, and Cr II 2066 lines, velocity centered on the Cr II 2056 line, while the bottom depicts fitting of the Zn II 2026, Cr II 2026, and Mg I 2026 lines, velocity centered on the Zn II line. This system has a redshift of 1.999.
Figure 13: Absorption line profile fitting for Q1331. The top figure represents fitting of the Cr II 2056, Cr II 2062, Zn II 2062, and Cr II 2066 lines, velocity centered on the Cr II 2056 line, while the bottom depicts fitting of the Zn II 2026, Cr II 2026, and Mg I 2026 lines, velocity centered on the Zn II line. This system has a redshift of 2.1776.
Figure 14: Absorption line profile fitting for Q2231. The top figure represents fitting of the Cr II 2056, Cr II 2062, Zn II 2062, and Cr II 2066 lines, velocity centered on the Cr II 2056 line, while the bottom depicts fitting of the Zn II 2026, Cr II 2026, and Mg I 2026 lines, velocity centered on the Zn II line. This system has a redshift of 2.066.
<table>
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<th>Si II</th>
<th>Zn II</th>
<th>Cr II</th>
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</table>

Table 5: Column Densities obtained from the profile fitting. H I column densities were available in the literature but others available in the literature were omitted in favor of the results from our profile fitting.
SECTION IV

DATA ANALYSIS

To further explore the correlation between $\text{[Si II / Mg I]}$ and $\text{[Zn II / H I]}$, we used statistical analysis software routines that are a part of the Space Telescope Science Data Analysis System (STSDAS). The STSDAS package, developed at the Space Telescope Science Institute, is part of a larger system developed by the National Optical Astronomical Observatory called the Image Reduction and Analysis Facility (IRAF). The two routines used to analyze the data, \texttt{bhkmethoed} and \texttt{schmittbin}, are discussed below.

**Kendall Tau Rank Correlation Coefficient**

In order to test whether or not these data are statistically correlated, we use the \texttt{bhkmethoed} routine in IRAF to calculate the Kendall Tau Rank Correlation Coefficient. The Kendall Tau is generally calculated via a method by which simple comparison is performed on the pairs of data and the pairs are categorized as either \textit{concordant} or
discordant (Nelson 2001⁹). A pair is considered concordant if, given pairs \((x_i, y_i)\) and \((x_j, y_j)\):

\[
x_i < x_j \text{ and } y_i < y_j \quad \text{or} \quad x_i > x_j \text{ and } y_i > y_j
\]

Conversely, a pair is said to be discordant if either of the following are true:

\[
x_i < x_j \text{ and } y_i > y_j \quad \text{or} \quad x_i > x_j \text{ and } y_i < y_j
\]

Let \(c\) equal the number of concordant pairs and \(d\) equal the number of discordant pairs.

The Kendall Tau is then defined as:

\[
\tau = \frac{c - d}{c + d}
\]

However, by the nature of these observations our data include upper limits and lower limits as well as detections. Therefore, we must use techniques referred to as survival analysis to account for this. The algorithms used in the STSDAS package employ survival analysis to handle censoring\(^{10}\) of data, taking into account lower limits (right censored), upper limits (left censored), and detections.

The method by which IRAF calculates the Kendall Tau coefficient, established by Brown, Hollander, and Korwar (1974), is slightly modified from that described above. Much detail about this procedure is described by Isobe, Feigelson, and Nelson (1986), including a sample calculation. Here, the coefficient for a data set of \(n\) points is defined as:

\[
\quad
\]

\[ \tau = \sum_{i=1}^{n} \sum_{j=1}^{n} a_{ij} b_{ij} \]

Where \( a_{ij} \) is equal to: 1 if \( x_i \) is definitely less than \( x_j \), -1 if \( x_i \) is definitely greater than \( x_j \), and 0 if the two are equal or if the comparison is uncertain.

Table 6 shows the data input into IRAF, including censoring flags. In cases where an upper limit was given for Mg I, the censoring reflects a lower limit since the calculation of \([\text{Si II} / \text{Mg I}]\) places this in the denominator. The specification of the censoring flags is given in Table 3.
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<th>[Si/Mg]</th>
<th>[Zn/H]</th>
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<td>1</td>
</tr>
<tr>
<td>Q0841+12</td>
<td>2.979</td>
<td>-1.43</td>
<td>1</td>
</tr>
<tr>
<td>J1237+0647</td>
<td>1.01</td>
<td>0.34</td>
<td>0</td>
</tr>
<tr>
<td>Q1215+33</td>
<td>3.6</td>
<td>-1.26</td>
<td>0</td>
</tr>
<tr>
<td>Q1331+17</td>
<td>2.5412</td>
<td>-1.2364</td>
<td>0</td>
</tr>
<tr>
<td>Q2231-00</td>
<td>2.857</td>
<td>-0.97</td>
<td>0</td>
</tr>
</tbody>
</table>

Table 6: Input table for survival analysis indicating censoring.
The bhkmethod routine outputs not only the Kendall Tau coefficient, but also a probability that a correlation does not exist (it assumes the null hypothesis). From our data, we calculate a Kendall Tau coefficient of -0.6115 and a 0.3% probability that a correlation does not exist.

**Schmitt's Binned Linear Regression**

To attempt a linear fit to our data, we used the schmittbin routine (also a part of the IRAF/STSDAS package). The mathematical procedure for this linear regression is given by Schmitt (1985). Here we merely state the result of the calculation. The result is a slope of $-0.5427 \pm 0.1249$ and an intercept of $2.1432 \pm 0.1524$. Figure 15 shows our data points overplotted with the result of this regression.
Figure 15: Plot of data sample with linear regression fit. Here, the red points indicate DLAs and blue points indicate Sub-DLAs.
SECTION IV

INTERPRETATION AND CONCLUSION

Statistically, the correlation we have measured between [Si II / Mg I] and [Zn II / H I] is quite convincing. However, the physical reasons giving rise to this correlation deserve investigation and in this section we present ensuing methods and possible scenarios responsible for this effect.

Photoionization Models

In an attempt to identify the physical conditions in DLAs and Sub-DLAs that result in the abundance ratio correlation, we ran several simulations of intergalactic gas clouds using the photoionization modeling software Cloudy.

Calculations were performed with version 08 of Cloudy, last described by Ferland et al. (1998). Figure 16 shows the result of a large simulation where we attempted to recreate the observed trend. Here, a grid of calculations were performed varying H I column density from 18.5 - 21.5 and metallicity from -2 to 1 (both sets of quantities in logarithmic scale).

\textsuperscript{11} Calculations were performed with version 08 of Cloudy, last described by Ferland et al. (1998).
Figure 16: Results of Cloudy photoionization model calculations that were completed using input values of N(HI) spanning from 18.5 to 21.5 and a range of metallicity values reflecting the range of our sample. Curves of constant metallicity are shown here connecting several points.
While a correlation does not clearly emerge as observed from our sample, this brought about some interesting questions regarding Cloudy’s treatment of certain physical parameters such as dielectronic recombination. As stated by de Boer et al. (1985), recombination increases sharply for Mg at ~5000 K. The question here was whether or not Cloudy was taking into effect this temperature dependence and thus impacting the calculated abundances of magnesium and silicon. A conference with Gary Ferland, Cloudy’s author, confirmed that temperature dependence was incorporated into the software.

**Dust Shielding**

Another possible cause of increased Mg I relative abundance with increasing metallicity is the presence of dust grains which shield ionizing photons. We may derive an estimated quantity of total dust grains by the following procedure. Since iron is generally heavily depleted, the abundance ratio [Fe / Zn] gives a measure of fraction of iron that remains in the gas phase. Therefore, the fraction settled onto dust grains should be given by one minus this quantity. We then add the relative abundance [Zn / H] and N(HI) to arrive the total column of Fe. Then the estimated number of grains should be:

\[ \text{grains} \propto 10^{\left(1 - [Fe/Zn] + [Zn/H] + N(HI)\right)} \]

We plot this quantity versus [Si II / Mg I] in figure 16.
Dust Grains vs. [Si II / Mg I]

Figure 17: Dust depletion (as measured by the [Cr / Zn] ratio) plotted against [Si II / Mg I].
Upon running the same Kendall Tau correlation procedure outlined above on this relationship, we found a result of \( \tau = 0.4494 \) which corresponds to a 3.08% probability that a correlation does not exist. Therefore, we are led to believe that dust shielding does play a role in the fact the higher metal-content (and higher dust-content) systems tend to exhibit more neutral magnesium.

**Neutral Hydrogen Dependence**

Lastly, we consider the relationship between H I column density and metallicity. We stated in Section 2 that Sub-DLAs are more likely to be metal rich than DLAs therefore our correlation between metallicity and [Si II / Mg I] could be biased because of the dearth of metal-rich DLAs and metal-poor Sub-DLAs discovered thus far. Figure 18 shows a three-dimensional plot where the “z-axis” is \( N(\text{H I}) \), indicating a decreasing metallicity with increasing neutral hydrogen.

Why would Sub-DLAs contain more Mg I? The answer may lie in the lesser amount of neutral gas within the system, thus greater ionization of the present hydrogen. With increased ionization overall, this would correspond to an increasing free electron density and increased likelihood of recombination. Isolating this free electron density as well as temperature (to account for the dielectronic recombination effect mentioned above) would prove necessary in the modeling process to recreate this trend.

Lastly, we conclude that more surveys of high column density absorbers will ultimately reveal the robustness of this trend. If metal poor Sub-DLAs are found to exist that do not exhibit this increasing neutral magnesium with increasing metallicity trend, it
will indicate a selection bias of metal-rich objects contributing to the perceived effect. Similarly, the discovery of metal-rich DLAs, possibly through increasingly blind surveys could also provide counterevidence. Objects observed until the present reveal few of these systems, although studies are taking place to examine potential selection effects. For instance, Fynbo et al. (2011) are looking at luminous galaxy counterparts to high column density absorbers and have discovered at least one metal rich system. As these types of observation programs are carried out, it will be particularly interesting to see if this reveals a plethora of metal-rich DLAs and where such metal rich DLAs exhibit increasing Mg I column density as do the Sub-DLAs.

Conclusion

In this work, we have examined a correlation that seems to exist between [Si II / Mg I] and metallicity (as measured in [Zn II / H I]) in DLAs and Sub-DLAs. Not only do we find that the correlation is statistically sound within our sample, but conclude that the presence of dust also contributes to increased neutral magnesium. However, the fact that known Sub-DLAs are relatively metal-rich as compared to DLAs may bias current samples as to enhance the effect seen here. As surveys continue to discover new and different high-column absorbers, usage of neutral magnesium as an easily measured proxy to trace the evolutionary history of metals in the gas and dust phase of the Universe will be further tested.
Figure 18: Similar to Figure 8, but the added dimension of neutral hydrogen column density. This plot
REFERENCES


Dyson, J. E. & Williams, D. A. (1980), Physics of the interstellar medium / J.E. Dyson ; D.A. Williams , Manchester University Press, Manchester :


Line Systems and Early Chemical Evolution', 108, 641-†.


CURRICULUM VITAE

Education

M.S. in Physics and Astronomy Expected graduation Spring 2011

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Thesis advisor: Dr. James T. Lauroesch

B.S. in Mathematics Spring 2005

Institution: University of Louisville

Concentration: Computational and Applied Mathematics

Current Research Areas

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Interactive Multimedia Public Outreach

Computer Experience

Astronomical: IDL, IRAF, Cloudy

Programming/scripting languages: C/C++, Visual Basic, Python, FORTRAN
Web-based development: XHTML, CSS, ASP.NET (C# and VB), Javascript, XSL

General: LaTeX, Linux OS, Extensive experience with Adobe Creative Suite Software

**Grants**

NASA Space Science Student Ambassador (2010-2011) $2600
Graduate Student Council Travel Award (2010) $300
Graduate Research and Creative Activities Grant (2010) $500
Graduate Student Council Travel Award (2009) $300

**Awards/Honors**

William Marshall Bullitt Award for the Best Student Paper in Astronomy/Astrophysics (UofL 2010) -

“Enhanced Public Outreach with Asteroseismology”

**Observing Experience**

6 nights using the Bok Telescope (2.1m) – Kitt Peak National Observatory

Medium-band imaging of Clowes-Campusano Large Quasar Group

**Academic Experience**

Graduate Teaching Assistant in Physics and Astronomy (U. of Louisville)

2009-Present

Position includes instruction of undergraduate laboratories and recitation sections
in general physics, kinematics and sound, electricity and magnetism, and general astronomy. Additional responsibilities include tutoring for all undergraduate physics courses as well as grading of exams and homework for large lecture sections.

Research Assistant (U. of Louisville) 2010

Projects have include investigating variability in time-separated QSO spectra (UVES) and ionization/metallicity correlation in Damped Lyman-α absorbers.

Author of Student Solutions Manual to Modern Physics for Scientists and Engineers 2010

This ancillary to the sophomore-level text in modern physics written by Dr. John C. Morrison and published by Elsevier includes descriptive, worked-out solutions to end-of-chapter problems.

Private Instrumental Music Instruction 2002-Present

I have professionally taught students of guitar, mandolin, and violin from all age groups and musical backgrounds.

Other Interests/Activities

Founding board member of Star Duck Charities, a 501(c)(3) nonprofit organization dedicated to improving the lives of at-risk orphan children. Fundraising efforts have raised over $50,000 for local youth.
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